## Probability Question Paper 4

| Level | International A Level |
| :--- | :--- |
| Subject | Maths |
| Exam Board | CIE |
| Topic | Probability |
| Sub Topic |  |
| Booklet | Question Paper 4 |


| Time Allowed: | $\mathbf{6 0}$ minutes |
| :--- | :--- |
| Score: | $/ 50$ |
| Percentage: | $/ 100$ |

Grade Boundaries:

| A* | A | B | C | D | E | U |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $>85 \%$ | $77.5 \%$ | $70 \%$ | $62.5 \%$ | $57.5 \%$ | $45 \%$ | $<45 \%$ |

1 There are three sets of traff c lights on Karinne's journey to work. The independent probabilities that Karinne has to stop at the frst , second and third set of lights are $0.4,0.8$ and 0.3 respectively.
(i) Draw a tree diagram to show this information.
(ii) Find the probability that Karinne has to stop at each of the frst two sets of lights but does not have to stop at the third set.
(iii) Find the probability that Karinne has to stop at exactly two of the three sets of lights.
(iv) Find the probability that Karinne has to stop at the f rst set of lights, given that she has to stop at exactly two sets of lights.

On any occasion when a particular gymnast performs a certain routine, the probability that she will perform it correctly is 0.65 , independently of all other occasions.
(i) Find the probability that she will perform the routine correctly on exactly 5 occasions out of 7 .
(ii) On one day she performs the routine 50 times. Use a suitable approximation to estimate the probability that she will perform the routine correctly on fewer than 29 occasions.
(iii) On another day she performs the routine $n$ times. Find the smallest value of $n$ for which the expected number of correct performances is at least 8 .

3 Two fair dice are thrown.
(i) Event $A$ is 'the scores differ by 3 or more'. Find the probability of event $A$.
(ii) Event $B$ is 'the product of the scores is greater than 8 '. Find the probability of event $B$.
(iii) State with a reason whether events $A$ and $B$ are mutually exclusive.

4 Boxes of sweets contain toffees and chocolates. Box $A$ contains 6 toffees and 4 chocolates, box $B$ contains 5 toffees and 3 chocolates, and box $C$ contains 3 toffees and 7 chocolates. One of the boxes is chosen at random and two sweets are taken out, one after the other, and eaten.
(i) Find the probability that they are both toffees.
(ii) Given that they are both toffees, fin the probability that they both came from box $A$.

5 When Andrea needs a taxi, she rings one of three taxi companies, $A, B$ or $C .50 \%$ of her calls are to taxi company $A, 30 \%$ to $B$ and $20 \%$ to $C$. A taxi from company $A$ arrives late $4 \%$ of the time, a taxi from company $B$ arrives late $6 \%$ of the time and a taxi from company $C$ arrives late $17 \%$ of the time.
(i) Find the probability that, when Andrea rings for a taxi, it arrives late.
(ii) Given that Andrea's taxi arrives late, f nd the conditional probability that she rang company $B$.

6 In a certain country $54 \%$ of the population is male. It is known that $5 \%$ of the males are colourblind and $2 \%$ of the females are colour-blind. A person is chosen at random and found to be colourblind. By drawing a tree diagram, or otherwise, find the probability that this person is male. [6]

7 Ivan throws three fair dice.
(i) List all the possible scores on the three dice which give a total score of 5, and hence show that the probability of Ivan obtaining a total score of 5 is $\frac{1}{36}$.
(ii) Find the probability of Ivan obtaining a total score of 7 .

